

Cross-Correlation of CFHTLenS Galaxy Catalogue and Planck CMB Lensing

A 5-month internship under the direction of Simon Prunet

Adrien Kuntz

Ecole Normale Supérieure, Paris

July 08, 2015

Outline

1 Introduction

2 Theoretical Cosmology

- Cosmological Perturbation Theory
- Gravitational Lensing and Galaxy Density
- Cross-Correlation
- The Halo Model

3 Data Maps

- Galaxies
- Convergence

4 Results

- Bayesian Analysis
- Consistency Checks

5 Conclusions

The Initial Motivation

Cross-Correlation of CFHTLenS Galaxy Number Density and Planck CMB Lensing

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¹*McGill University, QC, Canada, H3A2T8*

12 February 2015

ABSTRACT

We measure the cross-power spectrum between galaxy density from Canada-France-Hawaii-Telescope Lensing Survey (CFHTLenS) catalogues and gravitational lensing convergence from Planck data release 1 (2013) and 2 (2015). We investigate three main galaxy samples: $18.0 < i_{AB} < 22.0$, $18.0 < i_{AB} < 23.0$, $18.0 < i_{AB} < 24.0$ in the redshift range $0.2 < z < 1.3$ in each of the four CFHTLenS wide fields. By comparing the measured cross-spectrum with model predictions, linear galaxy-dark matter biases of $b = 0.82^{+0.24}_{-0.23}$, $0.83^{+0.19}_{-0.18}$, $0.82^{+0.16}_{-0.14}$ are inferred at significances of $3.5, 4.5, 5.6\sigma$ using the Planck 2015 release. These measurements are marginally consistent with biases derived from galaxy-galaxy auto-correlations: $b = 1.15^{+0.02}_{-0.01}$, $1.08^{+0.01}_{-0.01}$ and $0.96^{+0.01}_{-0.01}$ respectively. Using the 2013 Planck release, we obtain biases of $b = 1.33^{+0.29}_{-0.28}$, $1.19^{+0.23}_{-0.23}$, $1.16^{+0.19}_{-0.18}$, showing significant differences between the releases.

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- Achieve a good comprehension of the cosmological perturbation theory and of the halo model (*1 month 1/2*)
- Implement a python program to compute covariances from the halo model (*1 month 1/2*)
- Retrieve data from both the CFHTLenS and the Planck collaboration, format them in a sky map, and perform simulations (*1 month*)
- Use a bayesian analysis to fit galaxy bias from the correlation of the two maps (*1 week*)
- Write an insternship report and a presentation (*2 weeks*)

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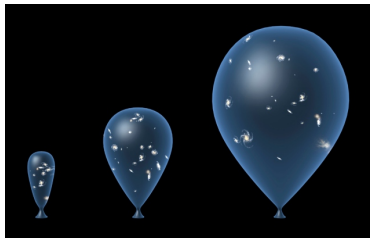
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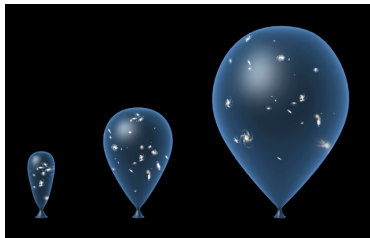
Friedmann-Lemaître Model



- $ds^2 = c^2 dt^2 - a^2(t) d\mathbf{x}^2$
- Physical coordinates : $\mathbf{r} = a(t) \mathbf{x}$
- Friedmann equations :

$$\begin{cases} \frac{\dot{a}^2 + kc^2}{a^2} = \frac{8\pi G\rho + \Lambda c^2}{3} \\ \frac{\ddot{a}}{a} = -\frac{4\pi G}{3} \left(\rho + \frac{3p}{c^2} \right) + \frac{\Lambda c^2}{3} \end{cases}$$
- Solution : $p = w\rho c^2 \Rightarrow \rho \propto a^{-3(1+w)}$

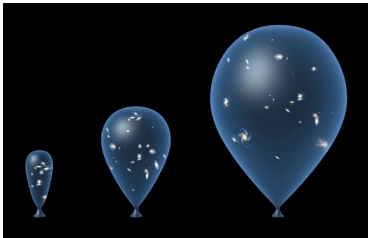
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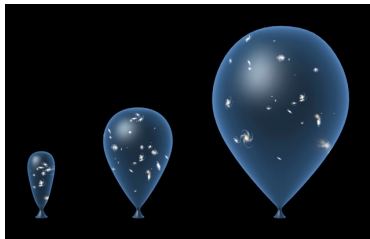
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Perturbation Theory

- $\rho(\mathbf{x}, t) \equiv \bar{\rho}(t) (1 + \delta(\mathbf{x}, t))$
- Linear solution : $\delta(\mathbf{x}, t) = D_1^+(t) A(\mathbf{x})$
- Non-linear solution : $\tilde{\delta}(\mathbf{k}, t) = \sum_{n=1}^{+\infty} a^n(t) \delta_n(\mathbf{k})$

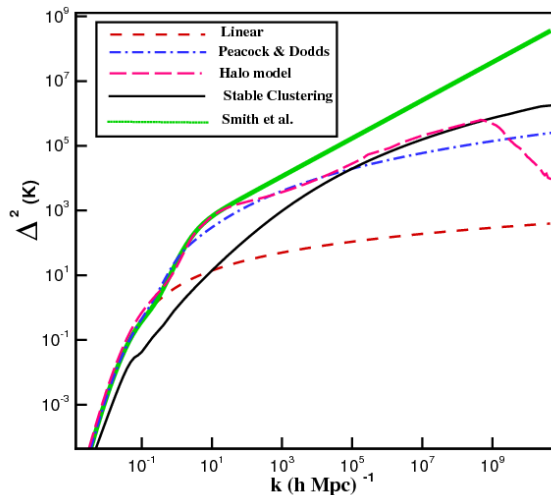
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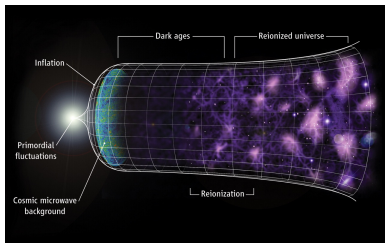
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Linear and Non-Linear Scales



Credit : Baghran et al (2011)

Correlation Function and Power Spectrum



- Primordial quantum fluctuations and inflation \Rightarrow Gaussian initial conditions

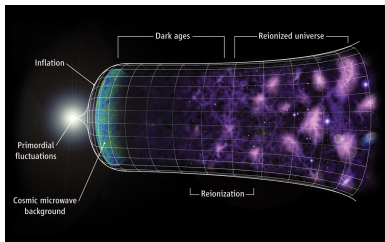
- Gravitational instability

- $\xi(r) = \langle \delta(\mathbf{x}) \delta(\mathbf{x} + \mathbf{r}) \rangle$

- $\langle \delta(\mathbf{k}) \delta(\mathbf{k}') \rangle = (2\pi)^3 \delta_D(\mathbf{k} + \mathbf{k}') P(k)$

- and higher order : B, T...

Correlation Function and Power Spectrum



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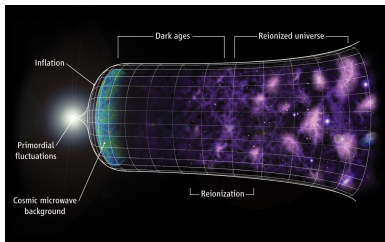
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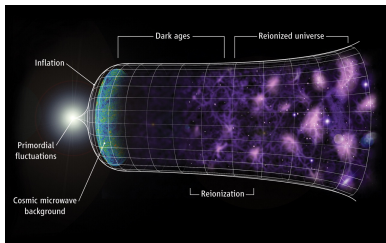
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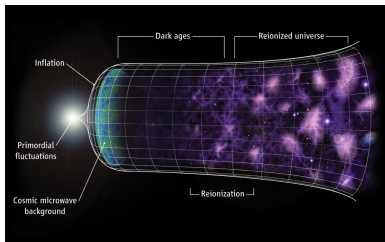
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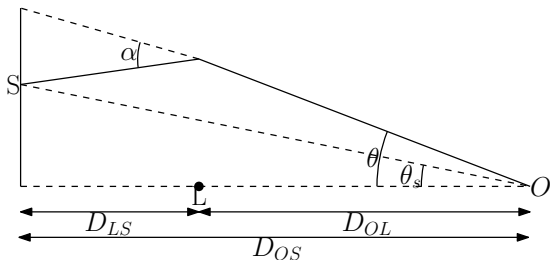


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Lens Equation



- α given in General Relativity
- Lens equation :
 $\theta = f(\theta_s)$

Illustration

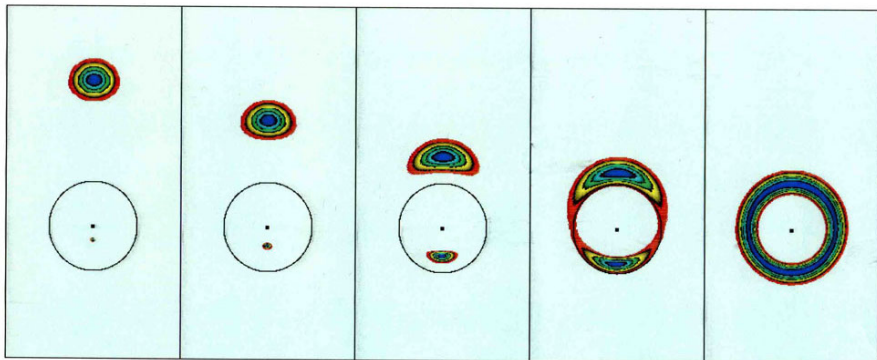
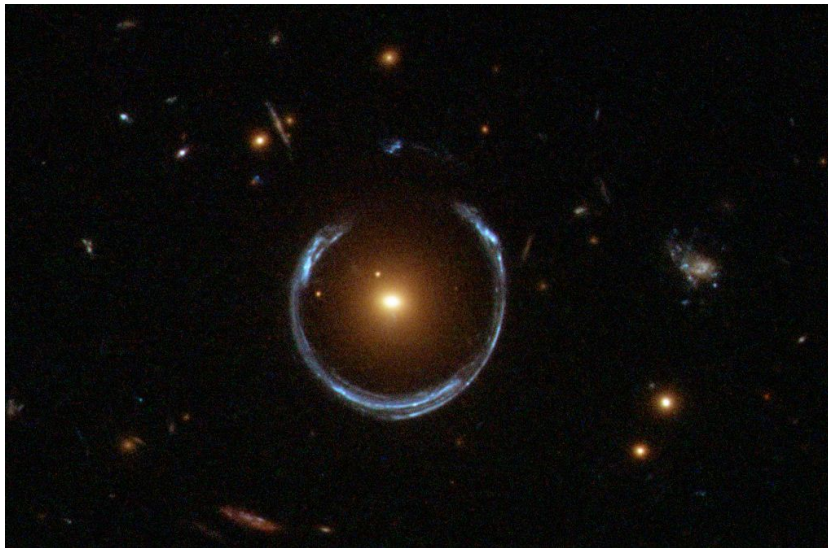
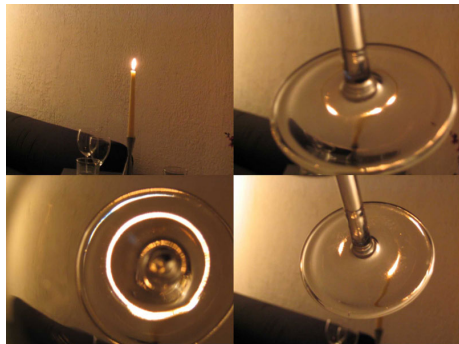
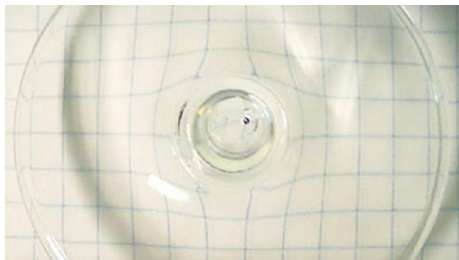


Figure: Distortion of an extended source by a point-like lens

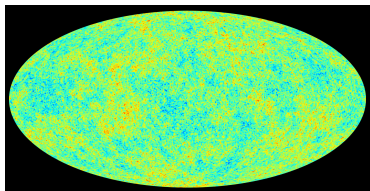
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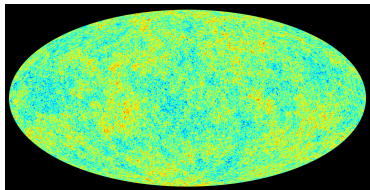
Effect on the CMB



- Deformation of the photon paths

- $\kappa(\theta) = \int_0^{\chi_{CMB}} W^\kappa(\chi) \delta(\chi\theta, \chi) d\chi$

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Galaxy Overdensity

- $\delta^{gal}(\chi\boldsymbol{\theta}, \chi) = b(\chi) \delta(\chi\boldsymbol{\theta}, \chi)$
- $g(\boldsymbol{\theta}) = \int_0^{\chi_{CMB}} W^g(\chi) \delta(\chi\boldsymbol{\theta}, \chi) d\chi$
- $W^g(\chi) \propto b(\chi)$

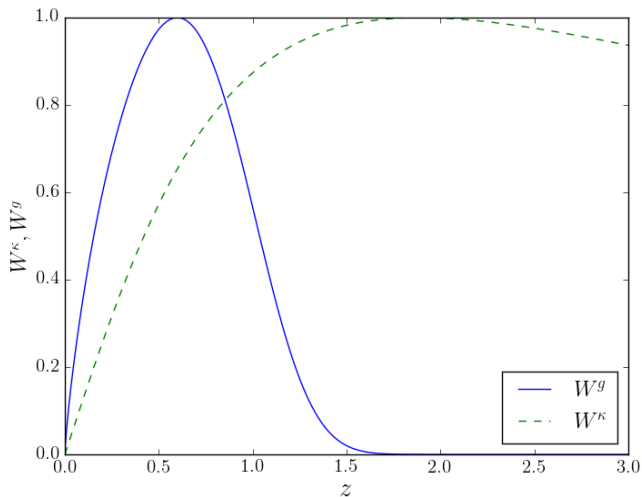
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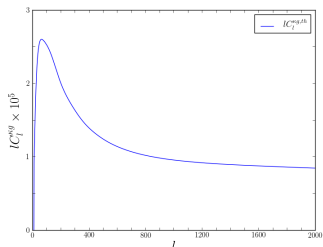
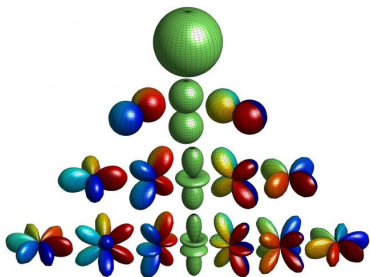
Lensing kernels



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Spherical Harmonics and Correlation



- $\kappa(\theta) \equiv \sum_{lm} \kappa_{lm} Y_l^m(\theta)$ and
 $g(\theta) \equiv \sum_{lm} g_{lm} Y_l^m(\theta)$

- $\langle \kappa_{lm} g_{l'm'}^* \rangle = \delta_{ll'} \delta_{mm'} C_l^{\kappa g}$

- $C_l^{\kappa g} = \int d\chi \frac{W^\kappa(\chi) W^g(\chi)}{\chi^2} P\left(k = \frac{l}{\chi}, z(\chi)\right)$

Covariance

- Covariance : $\Sigma_{ij}^{\kappa g} = \langle \tilde{C}_{l_i}^{\kappa g} \tilde{C}_{l_j}^{\kappa g} \rangle - \langle \tilde{C}_{l_i}^{\kappa g} \rangle \langle \tilde{C}_{l_j}^{\kappa g} \rangle$
- $\Sigma_{ij}^{\kappa g} = \text{Gaussian Term} + \text{Non-Gaussian Term}$
- Non-Gaussian term involves $T = \langle \delta(\mathbf{k}_1) \delta(\mathbf{k}_2) \delta(\mathbf{k}_3) \delta(\mathbf{k}_4) \rangle$

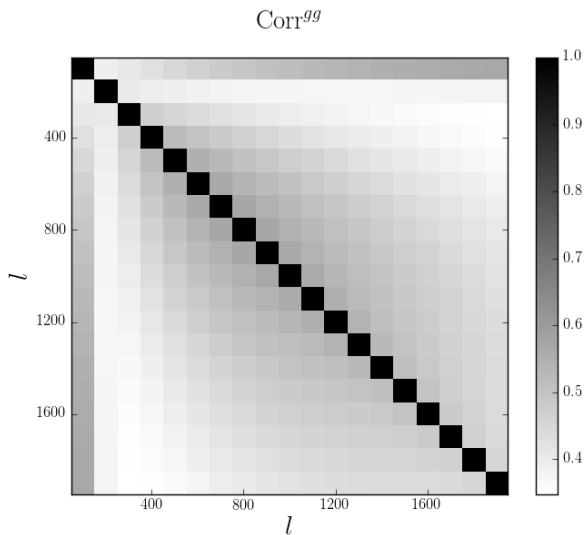
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Correlation Matrix



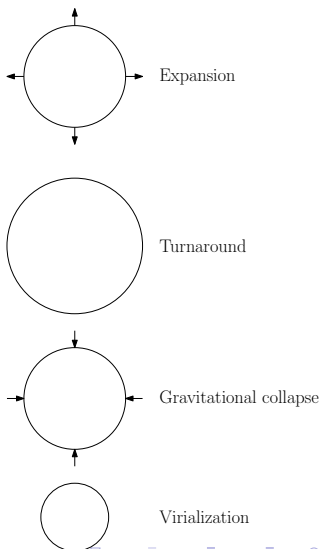
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Spherical Collapse

- $\delta_{sc} = 1.69$

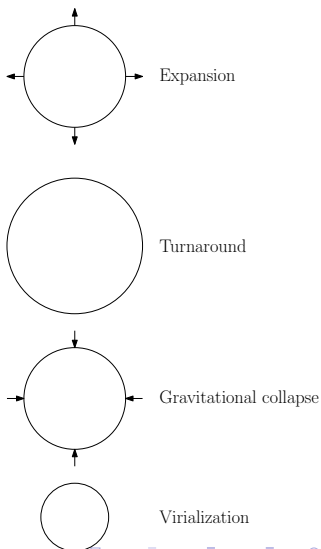
- $\rho_{halo} = \Delta_{sc} \rho_{background}, \Delta_{sc} \simeq 340$



Spherical Collapse

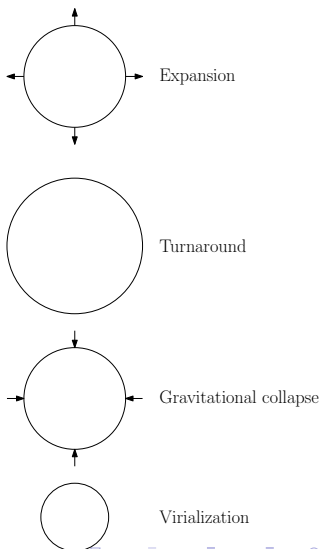
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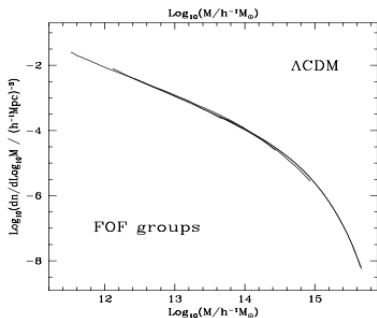


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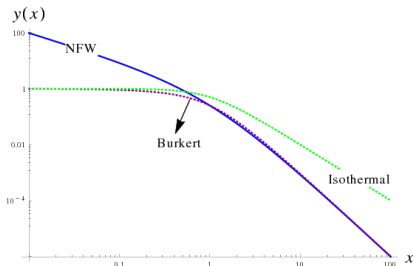
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Ingredients



$n(m, z)$ Press & Schechter (1974)

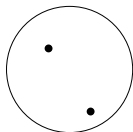


$\rho(r; m)$ NFW profile (1997)

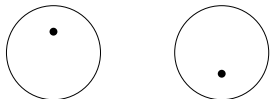
$$\delta_h(\mathbf{x}, z; m) = \sum_{k>0} b_k(m, z) \delta(\mathbf{x})^k / k! \text{ Mo \& White (1995)}$$

Correlation Function

1-halo



2-halo



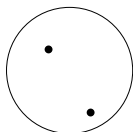
- $\rho_{tot}(\mathbf{x}) = \sum_i \rho(\mathbf{x} - \mathbf{x}_i, m_i)$

- $\xi(r) = \left\langle \frac{\rho(\mathbf{x})\rho(\mathbf{x}+\mathbf{r})}{\bar{\rho}^2} \right\rangle - 1$

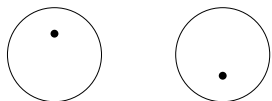
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1-halo term + 2-halo term

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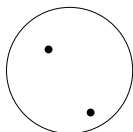
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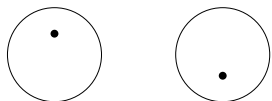
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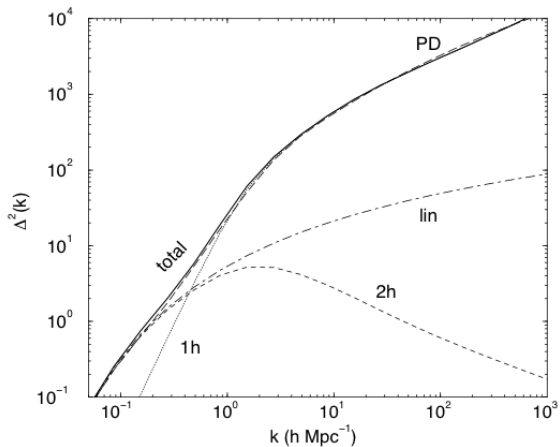


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Power Spectrum



Credit :
Cooray &
Sheth (2002)

Trispectrum

$$T_{hhhh}(\mathbf{k}_1, -\mathbf{k}_1, \mathbf{k}_2, -\mathbf{k}_2) = T^{1h} + T^{2h} + T^{3h} + T^{4h}$$

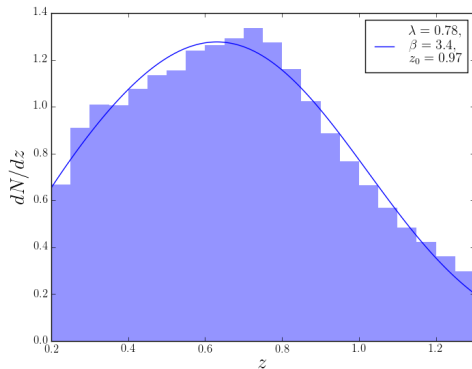
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The CFHTLenS Catalogue

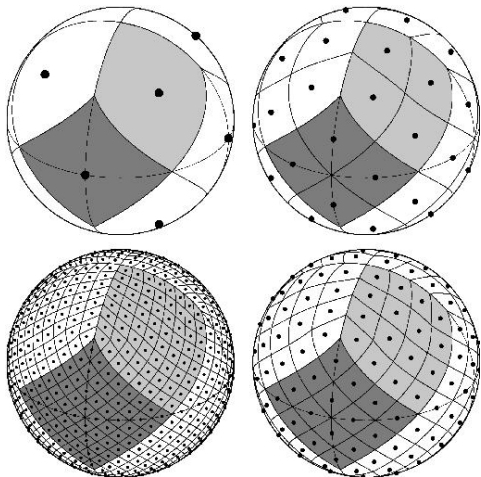
- Analysis of the CFHT Legacy Survey specialized in the production of a galaxy catalogue for lensing measurement
- CFHTLS : 171 MegaCam pointings 2003-2008, more than 2300 hours
- 4 patches, 154 deg²
- Galaxy catalogue and accurate photometric redshifts :
 $\sigma \sim 0.04(1+z)$
- $0.2 < z < 1.3$ and $18 < i_{AB} < 24$

Redshift Distribution



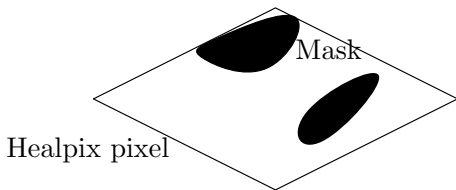
$$\frac{dN}{dz} = \frac{\alpha}{z_0} \left(\frac{z}{z_0}\right)^\lambda \exp\left(-\left(\frac{z}{z_0}\right)^\beta\right)$$

Healpix



- JPL / NASA
- Pixels of equal area
- Iso-latitude
- Interface in Python
- 1 pixel = 1.7 arcmin

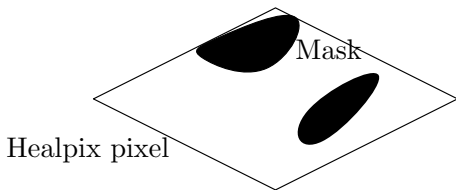
Mask



- Weight : $w_i = \frac{S_{unmasked}}{S_{tot}}$
- Galaxy overdensity :

$$\delta_i = \frac{N_i/w_i - \langle N \rangle}{\langle N \rangle}$$
- $\bar{n} = 15.1 \text{ gal} / \text{arcmin}^2$

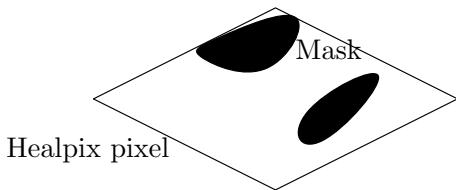
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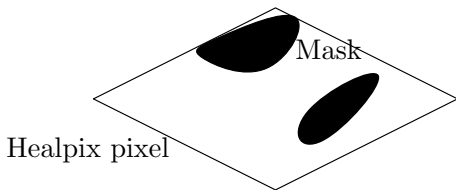
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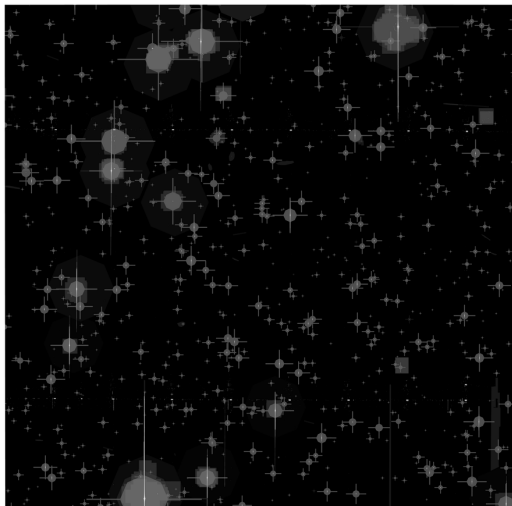
Mask



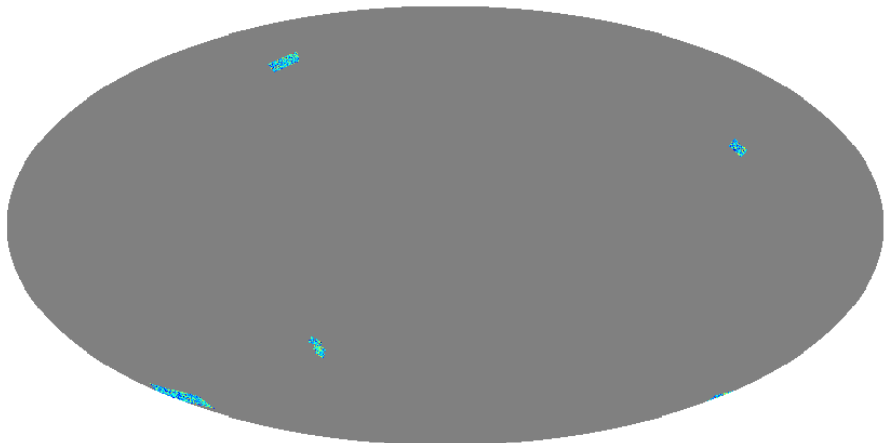
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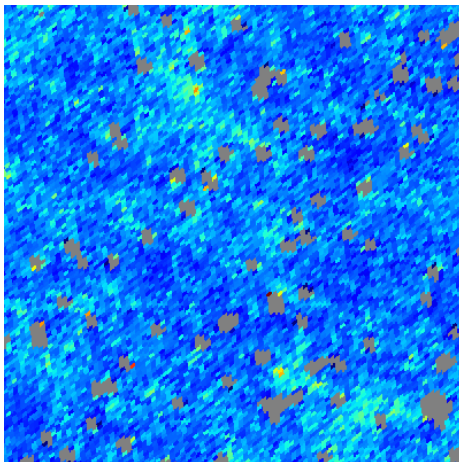
Mask



Galaxy Map



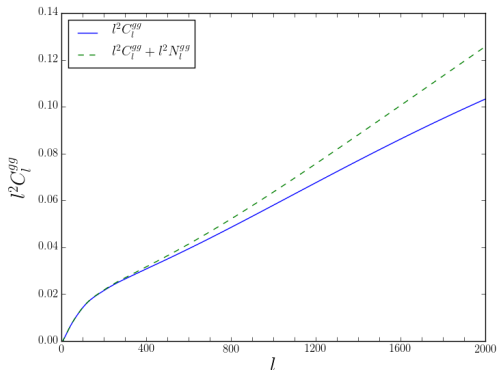
Galaxy Map



on (99.405,57.51)



Noise



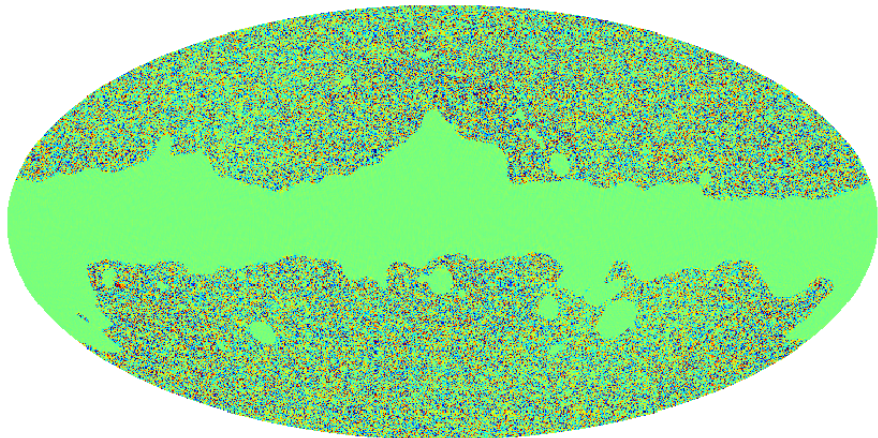
- Poisson process : shot noise
- $C_l^{gg} \rightarrow C_l^{gg} + N_l^{gg}$, $N_l^{gg} = 1/\bar{n}$
(\bar{n} in galaxies / steradian !)
- Small effect

Outline

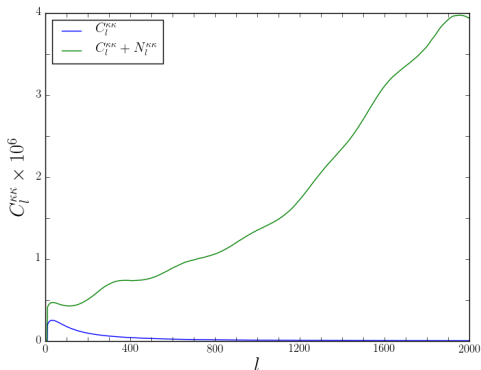
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Convergence Map

Mollweide view



Noise



- Obtained from the Planck simulations
- Dominant over C_l^{KK} !

A Consequence of the High Level of Noise

$$\Sigma_{ij}^{\kappa g} = \frac{1}{4\pi f_{sky}} \left[\frac{(2\pi)^2}{\Omega_i} \delta_{ij}^K \left((C_{l_i}^{\kappa\kappa} + N_{l_i}^{\kappa\kappa}) (C_{l_j}^{gg} + N_{l_j}^{gg}) + (C_{l_i}^{\kappa g})^2 \right) + \bar{T}_{ij}^{\kappa g} \right]$$

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Bayes Theorem

- $$\begin{cases} \tilde{C}_l^{\kappa g} = A \times b \times C_l^{\kappa g} \\ \tilde{C}_l^{gg} = b^2 \times C_l^{gg} \end{cases}$$

- $$P(A, b | \mathbf{C}) = \frac{P(A, b)P(\mathbf{C}|A, b)}{P(\mathbf{C})}$$

$$P(\mathbf{C} | A, b) = \mathcal{N} \exp \left\{ -\frac{1}{2} \left(\tilde{\mathbf{C}} - \mathbf{C}(A, b) \right) \Sigma^{-1} \left(\tilde{\mathbf{C}} - \mathbf{C}(A, b) \right) \right\}$$

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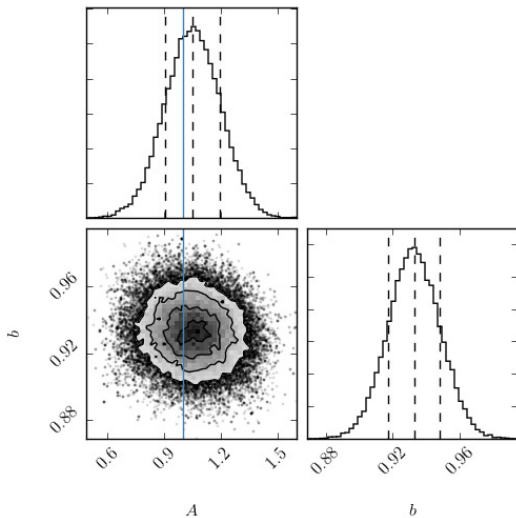
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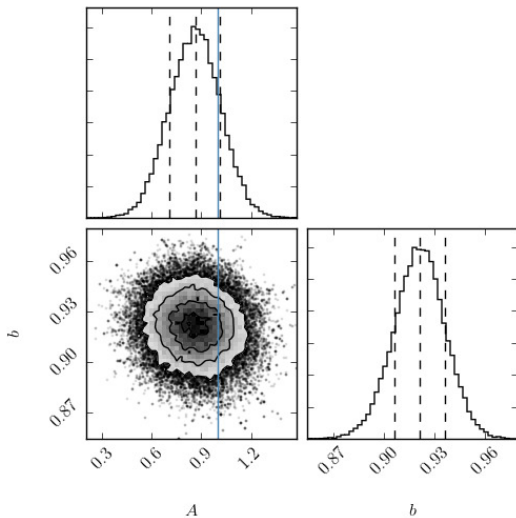
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MCMC 2013

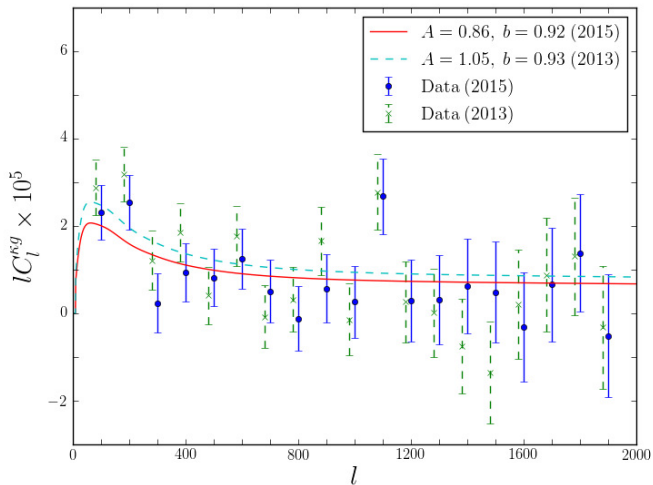


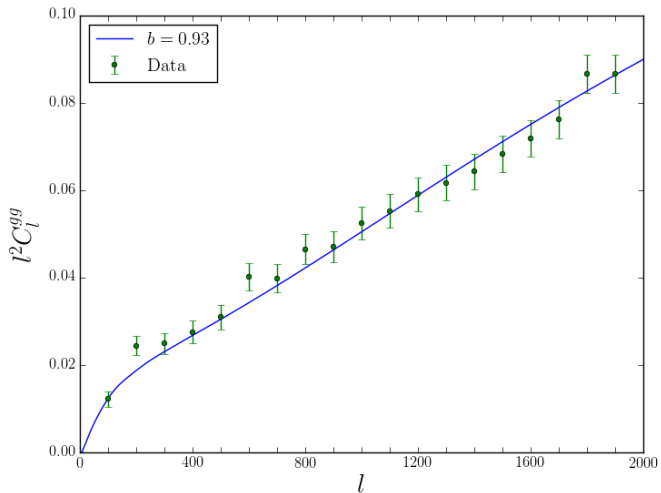
MCMC 2015



Best-Fit Values

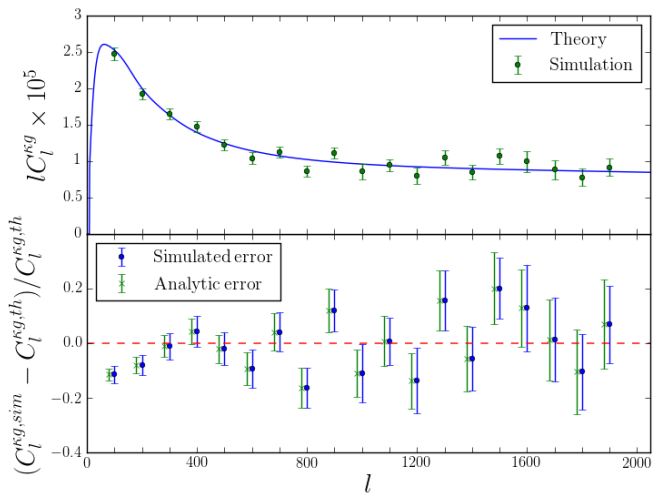
Patch	2013			2015		
	A	b	χ^2/ν	A	b	χ^2/ν
All	$1.05^{+0.15}_{-0.15}$	$0.93^{+0.02}_{-0.02}$	47.2/36	$0.86^{+0.15}_{-0.16}$	$0.92^{+0.02}_{-0.02}$	37.4/36

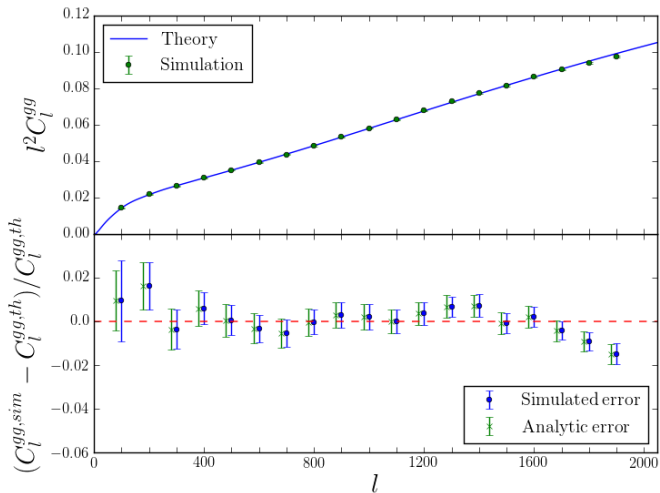


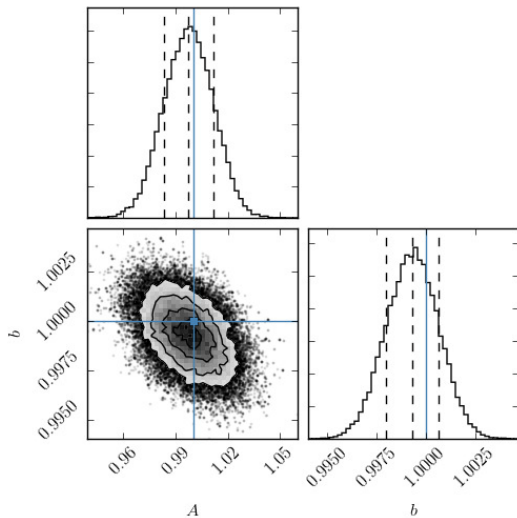


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$C_l^{\kappa g, simu}$




Recovered A and b 

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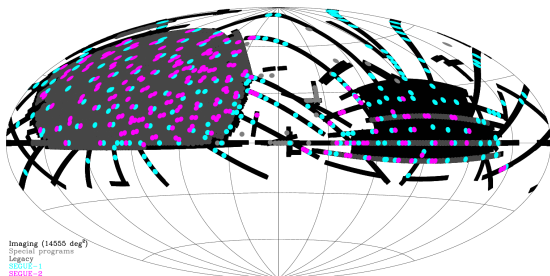
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Conclusions

- $b = 0.92_{-0.02}^{+0.02}$: good tracers of matter
- $A^{2013} = 1.05_{-0.15}^{+0.15}$ and $A^{2015} = 0.86_{-0.15}^{+0.15}$: compatible but different
- Partly confirm Omori & Holder (2015)

Forthcoming Work



- SDSS data : much better coverage of the sky
- If still a difference : investigate !

Questions ? Comments ?

Thank You CFHT !

